

* Claire Jones' PhD thesis, Edinburgh
(Gordon Plotkin)

Floyd static annotations
of flowchart programs

Standard, non-probabilistic

add non-determinism

add probability

Dijkstra logic of weakest
preconditions:
 $pre \Rightarrow wp(prog, post)$

Hoare logic of
sequential programs:
 $\{pre\} prog \{post\}$

Kozen logic of
probabilistic programs:
 $\{preE\} prog \{postE\}$

transformer model:
 $\mathbb{P}S \rightarrow \mathbb{P}S$
(conjunctive)

relational model:
 $S \rightarrow \mathbb{P}S$

relational model:
 $S \rightarrow S$

relational model:
 $S \rightarrow \text{dist}.S$

transformer model:
 $\text{fun}.S \rightarrow \text{fun}.S$
(linear)

Ancient, pre-1990*

Modern, post-1990*

transformer model:
 $\text{fun}.S \rightarrow \text{fun}.S$
(sublinear)

relational model:
 $S \rightarrow \mathbb{P}(\text{dist}.S)$

Inspired...
Is modelled by...
Generalises to...
Has a Galois connection between...

Probabilistic

Probability,
abstraction and
refinement

Quantitative mu-
calculus;
two-player games

Combined logic of weakest
pre-expectations:
 $preE \Rightarrow wp(prog, postE)$

Probabilistic process
algebras

...

add non-determinism and probability